

# Achieving Conflict Freedom in Norm-Based Societies

W. W. Vasconcelos<sup>[1,†]</sup>, M. J. Kollingbaum<sup>[1,\*]</sup>, A. García-Camino<sup>[2,◊]</sup>, and  
T. J. Norman<sup>[1,‡]</sup>

<sup>1</sup>Dept. of Computing Science, Univ. of Aberdeen, Aberdeen AB24 3UE, UK  
{\*mkolling,†wvasconc,‡tnorman}@csd.abdn.ac.uk  
<sup>2</sup>IIIA-CSIC, Campus UAB 08193 Bellaterra, Spain  
◊andres@iiia.csic.es

**Abstract.** Obligations, permissions and prohibitions, are a useful abstraction to specify and regulate the actions of self-interested software agents in open, heterogeneous systems. Any realistic account of such norms must address their dynamic nature: prohibitions can be lifted, obligations can be fulfilled and permissions can be revoked as a result of agents’ behaviours. These norms may at times *conflict* with one another, that is, an action may be simultaneously prohibited and obliged (or prohibited and permitted). In this paper, we present mechanisms to detect and resolve normative conflicts. We achieve more expressiveness, precision and realism in our norms by using *constraints* over first-order variables. The mechanism to detect and resolve norm conflicts takes into account such constraints and is based on first-order unification and constraint satisfaction. We also explain how the mechanisms can be deployed in the management of an explicit account of all norms associated with a society of agents.

## 1 Introduction

Norms such as obligations, permissions and prohibitions, are a useful abstraction to specify and regulate the observable behaviour of self-interested, heterogeneous software agents. Norms also support the establishment of organisational structures for coordinated resource sharing and problem solving [5, 13]. and regulate the behaviour of agents and impose restrictions and preferences on the choices from their behavioural repertoire. Norm-regulated VO’s may experience problems when norms assigned to agents are in *conflict* – actions that are forbidden, may, at the same time, be also obliged and/or permitted. For example, a norm “Agent  $X$  is permitted to  $send\_bid(ag_1, 20)$ ” and “Agent  $ag_2$  is prohibited from doing  $send\_bid(Y, Z)$ ” (where  $X, Y$  and  $Z$  are variables and  $ag_1, ag_2$  and 20 are constants) show two norms that are in conflict regarding an action  $send\_bid/2$ . Because normative conflicts may “paralyse” a software agent, seriously compromising its autonomy, we must provide means to automatically detect and resolve such conflicts.

In this paper, we propose a means to automatically detect and resolve norm conflicts. We make use of first-order unification [4] to find out if and how norms

overlap in their *scope of influence* [10]. If such a conflict is detected, a resolution can be found by proposing a *curtailment* of the conflicting norms. We curtail norms by adding constraints. For example, if we add constraint  $X \neq ag_2$  to the permission mentioned above, we curtail this norm such that it is relevant to any agent other than agent  $ag_2$ . The scope of influence of the permission becomes restricted and does not overlap with the influence of the prohibition – indicating a conflict-free situation between the two norms. Our curtailment mechanism operates at the level of an agent society and indicates a possible clarification of the normative situation for a set of agents.

In the following sections we provide an overview of a model of norm-governed agency and formally define concepts such as actions, norms and the global normative state of a society. Based on this model, we explain the detection and resolution of conflicts between norms, and provide algorithms for managing normative states of a society.

## 2 Norm-Governed Agency

Our model of norm-governed agency assumes that agents take on roles within a society or organisation and that these roles are determined by a set of norms. Roles, as used in, *e.g.*, [14], help us abstract from individual agents, defining a pattern of behaviour to which any agent that adopts a role ought to conform. We shall make use of two finite, non-empty sets,  $Agents = \{a_1, \dots, a_n\}$  and  $Roles = \{r_1, \dots, r_m\}$ , representing, respectively, the sets of agent identifiers and role labels. Central to our model is the concept of actions performed by agents:

**Definition 1.**  $\langle a : r, \bar{\varphi}, t \rangle$  represents a specific action  $\bar{\varphi}$  (a ground first-order formula), performed by  $a \in Agents$  adopting  $r \in Roles$  at time  $t \in \mathbb{N}$ .

Although agents are regarded as performing their actions in a distributed fashion (and, therefore, contributing to the enactment of the overall system), we propose a global account for all the actions taking place. It is, therefore, important to record the authorship of actions and the time when it occurs. The set  $\Xi$  is a set of such tuples recording actions of agents and represents a *trace* or a history of the enactment of a society of agents from a global point of view:

**Definition 2.** A global enactment state  $\Xi$  is a finite, possibly empty, set of tuples  $\langle a : r, \bar{\varphi}, t \rangle$ .

A global enactment state  $\Xi$  can be “sliced” into many partial states  $\Xi_a = \{\langle a : r, \bar{\varphi}, t \rangle \in \Xi \mid a \in Agents\}$  containing all actions of a specific agent  $a$ . Similarly, we could have partial states  $\Xi_r = \{\langle a : r, \bar{\varphi}, t \rangle \in \Xi \mid r \in Roles\}$ , representing the global state  $\Xi$  “sliced” across the various roles. We make use of a global enactment state to simplify our exposition; however, a fully distributed (and thus more scalable) account of enactment states can be achieved by slicing them as above and managing them distributedly.

## 2.1 Norm Specification

We adopt the notation of [15] for specifying norms, complementing it with *constraints* [9]. Constraints are used to *refine* the influence of norms on specific actions. We shall make use of numbers and arithmetic functions to build terms. Arithmetic functions may appear infix, following their usual conventions<sup>1</sup>. A syntax for constraints is introduced as follows:

**Definition 3.** *Constraints, represented as  $\gamma$ , are any construct of the form  $\tau \triangleleft \tau'$ , where  $\triangleleft \in \{=, \neq, >, \geq, <, \leq\}$ .*

Norms are then defined as follows:

**Definition 4.** *A norm  $\omega$  is a tuple  $\langle \nu, t_d, t_a, t_e \rangle$ , where  $\nu$  is any construct of the form  $O_{\tau_1:\tau_2}\varphi \wedge \bigwedge_{i=0}^n \gamma_i$  (an obligation),  $P_{\tau_1:\tau_2}\varphi \wedge \bigwedge_{i=0}^n \gamma_i$  (a permission) or  $F_{\tau_1:\tau_2}\varphi \wedge \bigwedge_{i=0}^n \gamma_i$  (a prohibition), where  $\tau_1, \tau_2$  are terms,  $\varphi$  is a first-order atomic formula and  $\gamma_i, 0 \leq i \leq n$ , are constraints. The elements  $t_d, t_a, t_e \in \mathbb{N}$  are, respectively, the time when  $\nu$  was declared (introduced), when  $\nu$  becomes active and when  $\nu$  expires,  $t_d \leq t_a \leq t_e$ .*

Term  $\tau_1$  identifies the agent(s) to whom the norm is applicable and  $\tau_2$  is the role of such agent(s).  $O_{\tau_1:\tau_2}\varphi \wedge \bigwedge_{i=0}^n \gamma_i$  thus represents an obligation on agent  $\tau_1$  taking up role  $\tau_2$  to bring about  $\varphi$ , subject to constraints  $\gamma_i, 0 \leq i \leq n$ . The  $\gamma_i$ 's express constraints on those variables occurring in  $\varphi$ . In the definition above we only cater for conjunctions of constraints. If disjunctions are required then a norm must be established for each disjunct. For instance, if we required the norm  $P_{A:R}move(A) \wedge A < 10 \vee A = 15$  then we must break it into two norms  $P_{A:R}move(A) \wedge A < 10$  and  $P_{A:R}move(A) \wedge A = 15$ . We assume an implicit universal quantification over variables in  $\nu$ . For instance,  $P_{A:R}p(X, b, c)$  stands for  $\forall A \in Agents. \forall R \in Roles. \forall X. P_{A:R}p(X, b, c)$ .

We propose to formally represent the normative positions of all agents, taking part in a virtual society, from a global perspective. By “normative position” we mean the “social burden” associated with individuals [7], that is, their obligations, permissions and prohibitions:

**Definition 5.** *A global normative state  $\Omega$  is a finite and possibly empty set of tuples  $\omega = \langle \nu, t_d, t_a, t_e \rangle$ .*

A global normative state, expressed by  $\Omega$ , complements the enactment state of a virtual society, expressed by  $\Xi$ , with information on the normative positions of individual agents. The management (*i.e.*, creation and updating) of global normative states is an interesting area of research. A simple but useful approach is reported in [6]: production rules generically depict how norms should be updated to reflect what agents have done and which norms currently hold. Similarly to  $\Xi$ , we use a single normative state  $\Omega$  to simplify our exposition; however, we can also slice  $\Omega$  into various sub-sets and manage them distributedly.

<sup>1</sup> We adopt Prolog's convention [1] using strings starting with a capital letter to represent variables and strings starting with a small letter to represent constants.

### 3 Norm Conflicts

We provide definitions for conflicts, their detection and resolution using constraints. Constraints confer more expressiveness and precision on norms, but the mechanisms for detection and resolution must factor them in. We use first-order unification [4] and constraint satisfaction [9] as the building blocks of our mechanisms. Initially, we define substitutions:

**Definition 6.** *A substitution  $\sigma$  is a finite and possibly empty set of pairs  $x/\tau$ , where  $x$  is a variable and  $\tau$  is a term.*

We define the application of a substitution in accordance with [4]. In addition, we describe how substitutions are applied to obligations, permissions and prohibitions (X stands for either O, P or F):

1.  $c \cdot \sigma = c$  for a constant  $c$ .
2.  $x \cdot \sigma = \tau \cdot \sigma$  if  $x/\tau \in \sigma$ ; otherwise  $x \cdot \sigma = x$ .
3.  $p^n(\tau_0, \dots, \tau_n) \cdot \sigma = p^n(\tau_0 \cdot \sigma, \dots, \tau_n \cdot \sigma)$ .
4.  $(X_{\tau_1:\tau_2} \varphi \wedge \bigwedge_{i=0}^n \gamma_i) \cdot \sigma = (X_{(\tau_1 \cdot \sigma):(\tau_2 \cdot \sigma)} \varphi \cdot \sigma) \wedge \bigwedge_{i=0}^n (\gamma_i \cdot \sigma)$ .
5.  $\langle \nu, t_d, t_a, t_e \rangle \cdot \sigma = \langle (\nu \cdot \sigma), t_d, t_a, t_e \rangle$

A substitution  $\sigma$  is a *unifier* of two terms  $\tau_1, \tau_2$ , if  $\tau_1 \cdot \sigma = \tau_2 \cdot \sigma$ . Unification is a fundamental problem in automated theorem proving and many algorithms have been proposed [4], recent work proposing means to obtain unifiers efficiently. We shall use unification in the following way:

**Definition 7.**  *$unify(\tau_1, \tau_2, \sigma)$  holds iff  $\tau_1 \cdot \sigma = \tau_2 \cdot \sigma$ , for some  $\sigma$ .*

The unification of atomic formulae is then defined as:

**Definition 8.**  *$unify(p^n(\tau_0, \dots, \tau_n), p^n(\tau'_0, \dots, \tau'_n), \sigma)$  holds iff  $unify(\tau_i, \tau'_i, \sigma), 0 \leq i \leq n$ .*

The *unify* relationship checks if a substitution  $\sigma$  is indeed a unifier for  $\tau_1, \tau_2$ , but it can also be used to find  $\sigma$ . We assume that *unify* is a suitable implementation of a unification algorithm which *i*) always terminates (possibly failing, if a unifier cannot be found); *ii*) is correct; and *iii*) has a linear computational complexity.

#### 3.1 Conflict Detection

Unification allows us to detect a conflict between norms. Norm conflict is formally defined as follows:

**Definition 9.** *A conflict arises between  $\omega, \omega' \in \Omega$  under a substitution  $\sigma$ , denoted as **conflict**( $\omega, \omega', \sigma$ ), iff the following conditions hold:*

1.  $\omega = \langle (F_{\tau_1:\tau_2} \varphi \wedge \bigwedge_{i=0}^n \gamma_i), t_d, t_a, t_e \rangle, \omega' = \langle (O_{\tau'_1:\tau'_2} \varphi' \wedge \bigwedge_{i=0}^n \gamma'_i), t'_d, t'_a, t'_e \rangle,$
2.  $unify(\langle \tau_1, \tau_2, \varphi \rangle, \langle \tau'_1, \tau'_2, \varphi' \rangle, \sigma), satisfy(\bigwedge_{i=0}^n \gamma_i \wedge (\bigwedge_{i=0}^m \gamma'_i \cdot \sigma))$
3.  $overlap(t_a, t_e, t'_a, t'_e).$

That is, a conflict occurs if *i*) a substitution  $\sigma$  can be found that unifies the variables of two norms<sup>2</sup>, and *ii*) the conjunction  $\bigwedge_{i=0}^n \gamma_i \wedge (\bigwedge_{i=0}^m \gamma'_i) \cdot \sigma$  of constraints from both norms can be satisfied<sup>3</sup> (taking  $\sigma$  under consideration), and *iii*) the activation period of the norms overlap. The *overlap* relationship holds if *i*)  $t_a \leq t'_a \leq t_e$ ; or *ii*)  $t'_a \leq t_a \leq t'_e$ .

For instance,  $P_{A:RP}(c, X) \wedge X > 50$  and  $F_{a:bp}(Y, Z) \wedge Z < 100$  are in conflict. We can obtain a substitution  $\sigma = \{A/a, R/b, Y/c, X/Z\}$  which shows how they overlap. Being able to construct such a unifier is a first indication that there may be a conflict or *overlap* of influence between both norms regarding the defined action. The constraints on the norms may restrict the overlap and, therefore, leave actions under certain variable bindings free of conflict. We, therefore, have to investigate the constraints of both norms in order to see if an overlap of the values indeed occurs. In our example, the permission has a constraint  $X > 50$  and the prohibition has  $Z < 100$ . By using the substitution  $X/Z$ , we see that  $50 < X < 100$  and  $50 < Z < 100$  represent ranges of values for variables  $X$  and  $Z$  where a conflict will occur.

For convenience (and without any loss of generality) we assume that our norms are in a special format: any non-variable term  $\tau$  occurring in  $\omega$  is replaced by a fresh variable  $X$  (not occurring anywhere in  $\omega$ ) and a constraint  $X = \tau$  is added to  $\omega$ . This transformation can be easily automated by scanning  $\omega$  from left to right, collecting all non-variable terms  $\{\tau_1, \dots, \tau_n\}$ ; then we add  $\bigwedge_{i=1}^n X_i = \tau_i$  to  $\nu$ . For example, norm  $P_{A:RP}(c, X) \wedge X > 50$  is transformed into  $P_{A:RP}(C, X) \wedge X > 50 \wedge C = c$ .

### 3.2 Conflict Resolution

In order to resolve a conflict, a machinery has to be put in place that computes a possible disambiguation of a normative situation – the set of norms  $\Omega$  has to be transformed into a set  $\Omega'$  that does not contain any conflicting norms so that the agent can proceed with its execution. In [19], this was achieved by annotating a norm with those values it cannot have. This process is called *curtailment* – one of the norms is changed in a way so that its scope of influence is reduced, leaving out specific values for the arguments of actions. By curtailing the scope of influence of a norm, the overlap between the two norms is eliminated. Differently from that work, we curtail norms by manipulating constraints. We formally define below how the curtailment of norms takes place. It is important to notice that the curtailment of a norm is a set of curtailed norms:

**Definition 10.** *Relationship curtail*( $\omega, \omega', \Omega$ ), where  $\omega = \langle X_{\tau_1:\tau_2} \varphi \wedge \bigwedge_{i=0}^n \gamma_i, t_d, t_a, t_e \rangle$  and  $\omega' = \langle X'_{\tau'_1:\tau'_2} \varphi' \wedge \bigwedge_{j=0}^m \gamma'_j, t'_d, t'_a, t'_e \rangle$  ( $X$  and  $X'$  being either  $O, F$  or

<sup>2</sup> A similar definition is required to address the case of conflict between a prohibition and a permission – the first condition should be changed to  $\omega' = \langle (P_{\tau'_1:\tau'_2} \varphi' \wedge \bigwedge_{i=0}^n \gamma'_i), t'_d, t'_a, t'_e \rangle$ . The rest of the definition remains the same.

<sup>3</sup> We assume an implementation of the *satisfy* relationship based on “off-the-shelf” constraint satisfaction libraries such as those provided by SICStus Prolog [18] and it holds if the conjunction of constraints is satisfiable.

P) holds iff  $\Omega$  is a possibly empty and finite set of norms obtained by curtailing  $\omega$  with respect to  $\omega'$ . The following cases arise:

1. If **conflict**( $\omega, \omega', \sigma$ ) does not hold then  $\Omega = \{\omega\}$ , that is, the curtailment of a non-conflicting norm  $\omega$  is  $\omega$  itself.
2. If **conflict**( $\omega, \omega', \sigma$ ) holds, then  $\Omega = \{\omega_0^c, \dots, \omega_m^c\}$ , where  $\omega_j^c = \langle X_{\tau_1:\tau_2}\varphi \wedge \bigwedge_{i=0}^n \gamma_i \wedge (\neg\gamma'_j \cdot \sigma), t_d, t_a, t_e \rangle$ ,  $0 \leq j \leq m$ .

In order to curtail  $\omega$ , thus avoiding any overlapping of values its variables may have with those variables of  $\omega'$ , we must “merge” the negated constraints of  $\omega'$  with those of  $\omega$ . Additionally, in order to ensure the appropriate correspondence of variables between  $\omega$  and  $\omega'$  is captured, we must apply the substitution  $\sigma$  obtained via **conflict**( $\omega, \omega', \sigma$ ) on the merged negated constraints.

By combining the constraints of  $\nu = X_{\tau_1:\tau_2}\varphi \wedge \bigwedge_{i=0}^n \gamma_i$  and  $\nu' = X_{\tau'_1:\tau'_2}\varphi' \wedge \bigwedge_{j=0}^m \gamma'_j$ , we obtain the curtailed norm  $\nu^c = X_{\tau_1:\tau_2}\varphi \wedge \bigwedge_{i=0}^n \gamma_i \wedge \neg(\bigwedge_{j=0}^m \gamma'_j \cdot \sigma)$ . The following equivalences hold:

$$X_{\tau_1:\tau_2}\varphi \wedge \bigwedge_{i=0}^n \gamma_i \wedge \neg(\bigwedge_{j=0}^m \gamma'_j \cdot \sigma) \equiv X_{\tau_1:\tau_2}\varphi \wedge \bigwedge_{i=0}^n \gamma_i \wedge (\bigvee_{j=0}^m \neg\gamma'_j \cdot \sigma)$$

That is,  $\bigvee_{j=0}^m (X_{\tau_1:\tau_2}\varphi \wedge \bigwedge_{i=0}^n \gamma_i \wedge \neg(\gamma'_j \cdot \sigma))$ . This shows that each constraint of  $\nu'$  leads to a possible solution for the resolution of a conflict and a possible curtailment of  $\nu$ . The curtailment thus produces a set of curtailed norms  $\nu_j^c = X_{\tau_1:\tau_2}p(t_1, \dots, t_n) \wedge \bigwedge_{i=0}^n \gamma_i \wedge \neg\gamma'_j \cdot \sigma$ ,  $0 \leq j \leq m$ .

Although each of the  $\nu_j^c$ ,  $0 \leq j \leq m$ , represents a solution to the norm conflict, we advocate that *all* of them have to be added to  $\Omega$  in order to replace the curtailed norm. This would allow a preservation of as much of the original scope of the curtailed norm as possible. As an illustrative example, let us suppose an  $\Omega$  with the following norm  $\omega$ ,

$$\Omega = \{\langle F_{A:RP}(C, X) \wedge C = c \wedge X > 50, t_d, t_a, t_e \rangle\}$$

If we try to introduce a new norm  $\omega' = \langle P_{B:Sp}(Y, Z) \wedge B = a \wedge S = r \wedge Z > 100, t'_d, t'_a, t'_e \rangle$  to  $\Omega$ , then indicates a conflict. This conflict can be resolved by curtailing one of the two conflicting norms. The constraints in  $\omega'$  are used to create such a curtailment. The new permission  $\omega'$  contains the following constraints:  $B = a$ ,  $S = r$  and  $Z > 100$ . Using  $\sigma$ , we construct copies of  $\omega$ , but adding  $\neg\gamma'_i \cdot \sigma$  to them. In our example the constraint  $Z > 100$  becomes  $\neg(Z > 100) \cdot \sigma$ , that is,  $X \leq 100$ . With the three constraints contained in  $\omega'$ , three options for curtailing  $\omega$  can be constructed. A new  $\Omega'$  is constructed, containing *all* the options for curtailment:

$$\Omega' = \left\{ \begin{array}{l} \langle P_{B:Sp}(Y, Z) \wedge B = a \wedge S = r \wedge Z > 100, t'_d, t'_a, t'_e \rangle \\ \langle F_{A:RP}(C, X) \wedge C = c \wedge X > 50 \wedge A \neq a, t_d, t_a, t_e \rangle \\ \langle F_{A:RP}(C, X) \wedge C = c \wedge X > 50 \wedge R \neq r, t_d, t_a, t_e \rangle \\ \langle F_{A:RP}(C, X) \wedge C = c \wedge X > 50 \wedge X \leq 100, t_d, t_a, t_e \rangle \end{array} \right\}$$

For each  $\neg\gamma'_i \cdot \sigma$  ( $A \neq a$ ,  $R \neq r$  and  $X \leq 100$  in our example), the original prohibition is extended with one of these constraints and added as a new, more restricted prohibition to  $\Omega'$ . Each of these options represents a part of the scope of influence regarding actions of the original prohibition  $\omega$ , restricted in a way

such that a conflict with the permission is avoided. In order to allow a check whether any other action that was prohibited by  $\omega$  is prohibited or not, it is necessary to make all three prohibitions available in  $\Omega'$ . If there are other conflicts, additional curtailments may be necessary.

### 3.3 An Implementation of Norm Curtailment

We show in Figure 1 a prototypical implementation of the curtailment process as a logic program. We show our logic program with numbered lines to enable the easy referencing of its constructs. Lines 1–7 define **curtail**, and lines 8–14 define

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1 curtail( $\omega, \omega', \Omega$ )  $\leftarrow$ 
2  $\omega = \langle X_{\tau_1:\tau_2} \varphi \wedge \bigwedge_{i=0}^n \gamma_i, t_d, t_a, t_e \rangle \wedge$ 
3  $\omega' = \langle X_{\tau'_1:\tau'_2} \varphi' \wedge \bigwedge_{j=0}^m \gamma'_j, t'_d, t'_a, t'_e \rangle \wedge$ 
4 conflict( $\omega, \omega', \sigma$ )  $\wedge$ 
5 merge( $[(\neg\gamma'_0 \cdot \sigma), \dots, (\neg\gamma'_m \cdot \sigma)], (\bigwedge_{i=0}^n \gamma_i), \widehat{\Gamma}) \wedge$ 
6 setof( $\langle X_{\tau_1:\tau_2} \varphi \wedge \Gamma, t_d, t_a, t_e \rangle, \text{member}(\Gamma, \widehat{\Gamma}), \Omega$ )
7 curtail( $\omega, \omega', \{\omega\}$ )

8 merge( $[], -, []$ )
9 merge( $[(\neg\gamma' \cdot \sigma) | Gs], (\bigwedge_{i=0}^n \gamma_i), [G|\widehat{\Gamma}]) \leftarrow$ 
10 satisfy( $(\bigwedge_{i=0}^n \gamma_i) \wedge (\neg\gamma' \cdot \sigma)$ )  $\wedge$ 
11  $\Gamma = (\bigwedge_{i=0}^n \gamma_i) \wedge (\neg\gamma' \cdot \sigma) \wedge$ 
12 merge( $Gs, (\bigwedge_{i=0}^n \gamma_i), \widehat{\Gamma})$ 
13 merge( $[-|Gs], (\bigwedge_{i=0}^n \gamma_i), \widehat{\Gamma}) \leftarrow$ 
14 merge( $Gs, (\bigwedge_{i=0}^n \gamma_i), \widehat{\Gamma})$ 

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**Fig. 1.** Implementation of **curtail** as a Logic Program

an auxiliary predicate *merge/3*. Lines 1–6 depict the case when the norms are in conflict: the test in line 4 ensures this. Line 5 invokes the auxiliary predicate *merge/3* which, as the name suggests, merges the conjunction of  $\gamma_i$ 's with the negated constraints  $\gamma'_j$ 's. Line 6 assembles  $\Omega$  by collecting the members  $\Gamma$  of the list  $\widehat{\Gamma}$  and using them to create curtailed versions of  $\omega$ . The elements of the list  $\widehat{\Gamma}$  assembled via *merge/3* are of the form  $(\bigwedge_{i=0}^n \gamma_i) \wedge (\neg\gamma'_j \cdot \sigma)$  – additionally, in our implementation we check if each element is satisfiable<sup>4</sup> (line 10). The rationale for this is that there is no point in creating a norm which will never be applicable as its constraints cannot be satisfied, so these are discarded during their preparation.

### 3.4 Curtailment Policies

Rather than assuming that a specific deontic modality is always curtailed<sup>5</sup>, we propose to explicitly use *policies* determining, given a pair of norms, which one is to be curtailed. Such policies confer more flexibility on our curtailment mechanism, allowing for a fine-grained control over how norms should be handled:

**Definition 11.** *A policy  $\pi$  is a tuple  $\langle \omega, \omega', (\bigwedge_{i=0}^n \gamma_i) \rangle$  establishing that  $\omega$  should be curtailed (and  $\omega'$  should be preserved), if  $(\bigwedge_{i=0}^n \gamma_i)$  hold.*

<sup>4</sup> In our implementation we made use of SICStus Prolog [18] constraint satisfaction libraries [9].

<sup>5</sup> In [19], for instance, prohibitions are always curtailed. This ensures the choices on the agents' behaviour are kept as open as possible.

A sample policy is  $\langle \langle F_{A:RP}(X, Y), T_d, T_a, T_e \rangle, \langle P_{A:RP}(X, Y), T'_d, T'_a, T'_e \rangle, (T_d < T'_d) \rangle$ . It expresses that any prohibition held by any agent that corresponds to the pattern  $F_{A:RP}(X, Y)$  has to be curtailed, if the additional constraint, which expresses that the prohibition's time of declaration  $T_d$  precedes that of the permission's  $T'_d$ , holds. Adding constraints to policies allows us a fine-grained control of conflict resolution, capturing classic forms of deontic conflict resolution – the constraint in the example establishes a precedence relationship between the two norms known as *legis posterior* (see section 4 for more details). We represent a set of policies as  $\Pi$ .

### 3.5 Management of Normative States

We present in Figure 2 an algorithm describing how an existing conflict-free set  $\Omega$  can be extended to accommodate a new norm  $\omega$ . The algorithm makes use of

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algorithm adoptNorm( $\omega, \Omega, \Pi, \Omega'$ )
input  $\omega, \Omega, \Pi$ 
output  $\Omega'$ 
begin
   $\Omega' := \emptyset$ 
  if  $\Omega = \emptyset$  then  $\Omega' := \Omega \cup \{\omega\}$ 
  else
    for each  $\omega' \in \Omega$  do
      if unify( $\omega, \omega', \sigma$ ) then
        if  $\langle \omega_\pi, \omega'_\pi, (\bigwedge_{i=0}^n \gamma_i) \rangle \in \Pi$  and unify( $\omega, \omega_\pi, \sigma$ ) and
          unify( $\omega', \omega'_\pi, \sigma$ ) and satisfy( $\bigwedge_{i=0}^n (\gamma_i \cdot \sigma)$ )
        then
          curtail( $\omega, \omega', \Omega''$ )
           $\Omega' := \Omega \cup \Omega''$ 
        else
          if  $\langle \omega'_\pi, \omega_\pi, (\bigwedge_{i=0}^n \gamma_i) \rangle \in \Pi$  and unify( $\omega, \omega_\pi, \sigma$ ) and
            unify( $\omega', \omega'_\pi, \sigma$ ) and satisfy( $\bigwedge_{i=0}^n (\gamma_i \cdot \sigma)$ )
          then
            curtail( $\omega', \omega, \Omega''$ )
             $\Omega' := (\Omega - \{\omega'\}) \cup (\{\omega\} \cup \Omega'')$ 
          endif
        endif
      endif
    endfor
  endif
end

```

**Fig. 2.** Norm Adoption Algorithm

a set  $\Pi$  of policies determining how the curtailment of conflicting norms should be done. Policies determine whether the new norm  $\omega$  is curtailed in case of a conflict or whether a curtailment of one of the existing  $\omega' \in \Omega$  should be done. When a norm is curtailed, a set of new norms replace the original norm. This set of norms is collected into  $\Omega''$  by **curtail**( $\omega, \omega', \Omega''$ ). A curtailment takes place if there is a conflict between  $\omega$  and  $\omega'$ . This test creates a unifier  $\sigma$  that is re-used in the policy test. When checking for a policy that is applicable, the algorithm uses unification to check (a) whether  $\omega$  matches/unifies with  $\omega_\pi$  and  $\omega'$  with  $\omega'_\pi$ ; and (b) whether the policy constraints hold under the given  $\sigma$ . If a previously agreed policy in  $\Pi$  determines that the newly adopted norm  $\omega$  is to be curtailed

in case of a conflict with an existing  $\omega' \in \Omega$ , then the new set  $\Omega'$  is created by adding  $\Omega''$  (the curtailed norms) to  $\Omega$ . If the policy determines a curtailment of an existing  $\omega' \in \Omega$  when a conflict arises with the new norm  $\omega$ , then a new set  $\Omega'$  is formed by *a)* removing  $\omega'$  from  $\Omega$  and *b)* adding  $\omega$  and the set  $\Omega''$ .

As well as adding norms to normative states we also need to support their removal. Since the introduction of a norm may have interfered with other norms, resulting in their curtailment, when that norm is removed we must *undo* the curtailments it caused, that is, we must *roll back* the normative state to a previous form. In order to allow curtailments of norms to be undone, we record the complete *history* of normative states representing the evolution of normative positions of agents:

**Definition 12.**  $\mathcal{H}$  is a non-empty and finite sequence of tuples  $\langle i, \Omega, \omega, \pi \rangle$ , where  $i \in \mathbb{N}$  represents the order of the tuples,  $\Omega$  is a normative state,  $\omega$  is a norm and  $\pi$  is a policy.

We shall denote the empty history as  $\langle \rangle$ . We define the concatenation of sequences as follows: if  $\mathcal{H}$  is a sequence and  $h$  is a tuple, then  $\mathcal{H} \bullet h$  is a new sequence consisting of  $\mathcal{H}$  followed by  $h$ . Any non-empty sequence  $\mathcal{H}$  can be decomposed as  $\mathcal{H} = \mathcal{H}' \bullet h \bullet \mathcal{H}''$ ,  $\mathcal{H}'$  and/or  $\mathcal{H}''$  possibly empty. The following properties hold for our histories  $\mathcal{H}$ :

1.  $\mathcal{H} = \langle 0, \emptyset, \omega, \pi \rangle \bullet \mathcal{H}'$
2.  $\mathcal{H} = \mathcal{H}' \bullet \langle i, \Omega', \omega', \pi' \rangle \bullet \langle i + 1, \Omega'', \omega'', \pi'' \rangle \bullet \mathcal{H}''$
3.  $\text{adoptNorm}(\omega_i, \Omega_i, \{\pi_i\}, \Omega_{i+1})$

The first condition establishes the first element of a history to be an empty  $\Omega$ . The second condition establishes that the tuples are completely ordered on their first component. The third condition establishes the relationship between any two consecutive tuples in histories: normative state  $\Omega_{i+1}$  is obtained by adding  $\omega_i$  to  $\Omega_i$  adopting policy  $\pi_i$ .

$\mathcal{H}$  is required to allow the retraction of a norm in an ordered fashion, as not only the norm itself has to be removed but also all the curtailments it caused when it was introduced in  $\Omega$ .  $\mathcal{H}$  contains a tuple  $\langle i, \Omega, \omega, \pi \rangle$  that indicates the introduction of norm  $\omega$  and, therefore, provides us with a normative state  $\Omega$  *before* the introduction of  $\omega$ . The effect of the introduction of  $\omega$  can be reversed by using  $\Omega$  and redoing (performing a kind of *roll-forward*) all the inclusions of norms according to the sequence represented in  $\mathcal{H}$  via *adoptNorm*.

This mechanism is detailed in Figure 3 as algorithm *removeNorm* describing how to remove a norm  $\omega$  given a history  $\mathcal{H}$ ; the algorithm outputs a normative state  $\Omega$  and an updated history  $\mathcal{H}'$  and works as follows. Initially, the algorithm checks if  $\omega$  indeed appears in  $\mathcal{H}$  – it does so by matching  $\mathcal{H}$  against a pattern of a sequence in which  $\omega$  appears as part of a tuple (notice that the pattern initialises the new history  $\mathcal{H}'$ ). If there is such a tuple in  $\mathcal{H}$ , then we initialise  $\Omega$  as  $\Omega_k$ , that is, the normative state *before*  $\omega$  was introduced. Following that, the **for** loop implements a *roll forward*, whereby new normative states (and associated history  $\mathcal{H}'$  are computed by introducing the  $\omega_i, k + 1 \leq i \leq n$ , which come after

```

algorithm removeNorm( $\omega, \mathcal{H}, \Omega, \mathcal{H}'$ )
input  $\omega, \mathcal{H}$ 
output  $\Omega, \mathcal{H}'$ 
begin
  if  $\mathcal{H} = \mathcal{H}' \bullet \langle k, \Omega_k, \omega, \pi_k \rangle \bullet \dots \bullet \langle n, \Omega_n, \omega_n, \pi_n \rangle$ 
  then
     $\Omega := \Omega_k$ 
    for  $i = k + 1$  to  $n$  do
      adoptNorm( $\omega_i, \Omega, \{\pi_i\}, \Omega'$ )
       $\mathcal{H}' := \mathcal{H}' \bullet \langle i, \Omega, \omega_i, \pi_i \rangle$ 
       $\Omega := \Omega'$ 
    endfor
  else
     $\mathcal{H} = \mathcal{H}'' \bullet \langle n, \Omega_n, \omega_n, \pi_n \rangle$ 
     $\Omega := \Omega_n, \mathcal{H}' := \mathcal{H}$ 
  end

```

**Fig. 3.** Algorithm to Remove Norms

$\omega$  in the original history  $\mathcal{H}$ . If  $\omega$  does not occur in any of the tuples of  $\mathcal{H}$  (this case is catered by the **else** of the **if** construct) then the algorithm uses pattern-matching to decompose the input history  $\mathcal{H}$  and obtain its last tuple – this is necessary as this tuple contains the most recent normative state  $\Omega_n$  which is assigned to  $\Omega$ ; the new history  $\mathcal{H}'$  is the same as  $\mathcal{H}$ .

## 4 Related Work

The work presented in this paper is an adaptation and extension of [19, 11] and [8], also providing a logic-theoretic investigation into deontic modalities for representing normative concepts [2, 17]. In [19], a conflict detection and resolution based on unification is introduced: we build on that research, introducing constraints to the mechanisms proposed in that work.

Efforts to keep law systems conflict-free can be traced back to the jurisprudential practice in human society. Inconsistency in law is an important issue and legal theorists use a diverse set of terms such as, for example, normative inconsistencies/conflicts, antinomies, discordance, etc., in order to describe this phenomenon. There are three classic strategies for resolving deontic conflicts by establishing a precedence relationship between norms: *legis posterior* – the most recent norm takes precedence, *legis superior* – the norm imposed by the strongest power takes precedence, and *legis specialis* – the most specific norm takes precedence [12]. The work presented in [11] discusses a set of conflict scenarios and conflict resolution strategies, among them the classic strategies mentioned above. For example, one of these conflict resolution strategies achieves a resolution of a conflict via negotiation with a norm issuer. In [3], an analysis of different normative conflicts is provided. The authors suggest that a deontic inconsistency arises when an action is simultaneously permitted and prohibited. In [16], three forms of conflict/inconsistency are described as *total-total*, *total-partial* and *intersection*. These are special cases of the intersection of norms as described in [11] – a permission entailing the prohibition, a prohibition entailing the permission or an overlap of both norms.

## 5 Conclusions & Future Work

We have presented a novel mechanism to detect and resolve conflicts in norm-regulated environment. Such conflicts arise when an action is simultaneously obliged and prohibited or, alternatively, when an action is permitted and prohibited. We introduce norms as first-order atomic formulae to whose variables we can associate arbitrary constraints – this allows for more expressive norms, with a finer granularity and greater precision. The proposed mechanism is based on first-order unification and constraint satisfaction algorithms, extending the work of [19], addressing a more expressive class of norms. Our conflict resolution mechanism amounts to manipulating the constraints of norms to avoid overlapping values of variables – this is called the “curtailment” of variables/norms. A prototypical implementation of the curtailment process is given as a logic program and is used in the management of the normative state of an agent society. We have also introduced an algorithm to manage the adoption of possibly conflicting norms, whereby explicit policies depict how the curtailment between specific norms should take place, as well as an algorithm depicting how norms should be removed, thus un-doing the effects of past curtailments.

We are currently exploiting our approach in mission-critical scenarios [20], including, for instance, combat and disaster recovery (*e.g.* extreme weather conditions and urban terrorism). Our goal is to describe mission scripts as sets of norms: these will work as contracts that teams of (human and software) agents can peruse and make sense of. Mission-critical contracts should allow for the delegation of actions and norms, via pre-established relationships between roles: we have been experimenting with special “count as” operators which neatly capture this. Additionally, our mission-critical contracts should allow the representation of plan scripts with the breakdown of composite actions down to the simplest atomic actions. Norms associated with composite actions will be distributed across the composite actions, possibly being delegated to different agents and/or roles.

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